

(#1)
P. 20

Given

$$\overline{BD} \perp \overline{AC}$$

def of \perp
segs

$$\angle ADB \text{ and } \angle CDB \text{ are rt}$$

All rt \angle s
are \cong

$$\angle ADB \cong \angle CDB$$

Given

$$\overline{AD} \cong \overline{CD}$$

Reflexive prop.

$$\overline{BD} \cong \overline{BD}$$

$$\triangle ABD \cong \triangle CBD$$

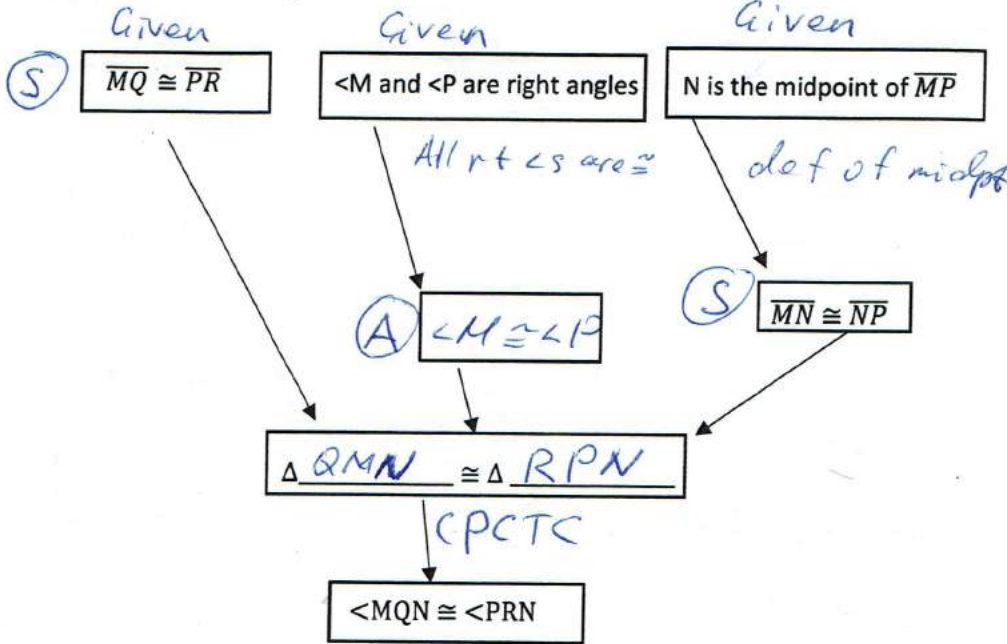
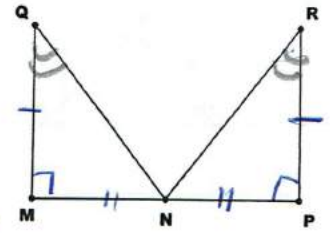
CPCTC

$$\angle ABD \cong \angle CBD$$

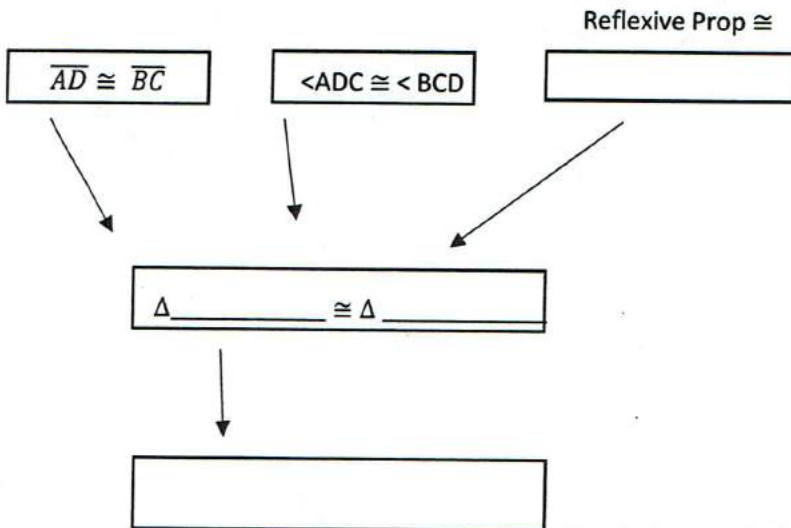
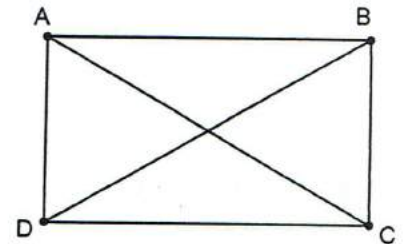
Practice with Proof

Ex 1) Given: $\overline{MQ} \cong \overline{PR}$, $\angle M$ and $\angle P$ are right angles.
 N is the midpoint of \overline{MP}

Prove: $\angle MQN \cong \angle PRN$

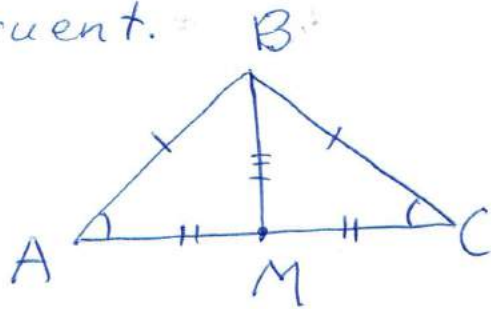


Ex 2) Given: $\overline{AD} \cong \overline{BC}$
 $\angle ADC \cong \angle BCD$
 Prove: $\overline{AC} \cong \overline{BD}$



Isosceles Triangle Theorem

If two sides of a triangle are congruent, then the angles opposite to these sides are congruent.



ITT

Given

$$\textcircled{S} \overline{AB} \cong \overline{BC}$$

M is midpt of \overline{AC}

def of midpt

$$\textcircled{S} \overline{AM} \cong \overline{MC}$$

SSS

Reflexive prop

$$\textcircled{S} \overline{BM} \cong \overline{BM}$$

$$\Delta ABM \cong \Delta CBM$$

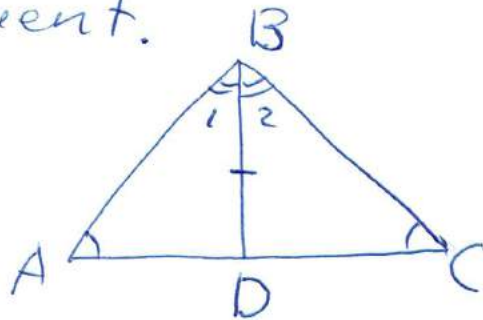
CPCTC

$$\angle A \cong \angle C$$

ITT Converse

If two angles of a triangle are congruent, then the sides opposite those angles are congruent.

ITT Converse



Given:

$$\angle A \cong \angle C$$

$$\text{Pr: } \overline{AB} \cong \overline{BC}$$

BD bisects $\angle ABC$

(A) $\angle A \cong \angle C$

(A) $\angle 1 \cong \angle 2$

(S) $\overline{BD} \cong \overline{BD}$ Reflexive prop

$$\triangle ABD \cong \triangle CBD$$

CPCTC

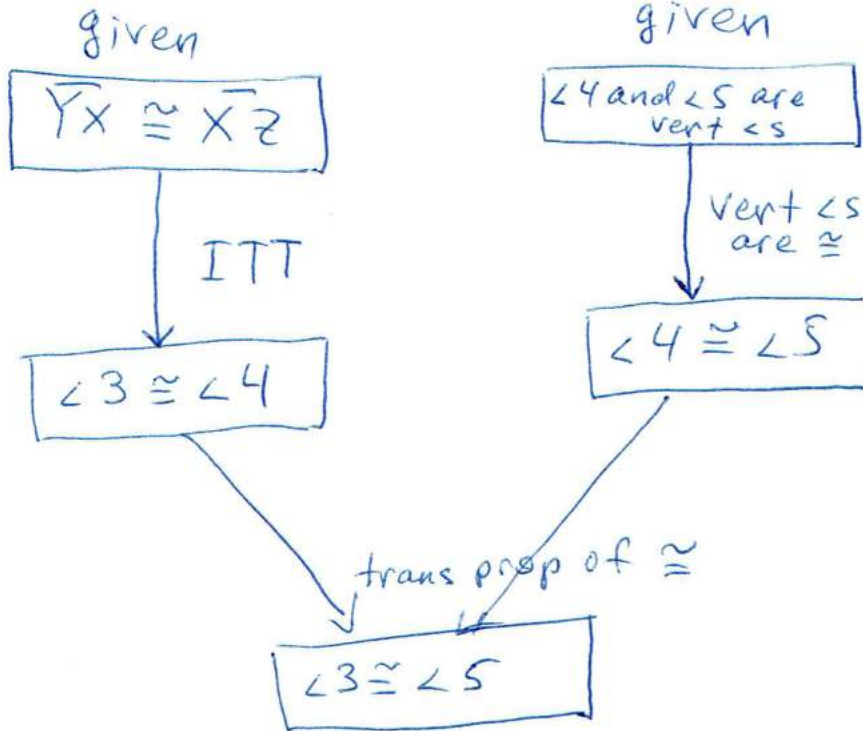
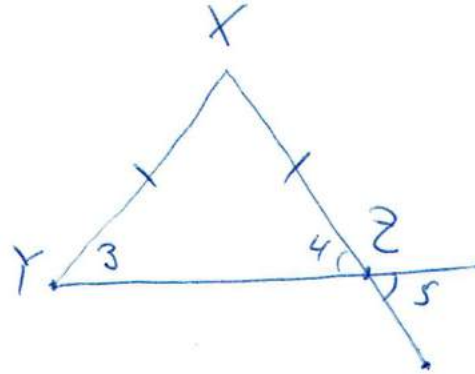
$$\overline{AB} \cong \overline{BC}$$

P24

#1

Given: $\overline{YX} \cong \overline{XZ}$

Prove: $\angle 3 \cong \angle 5$



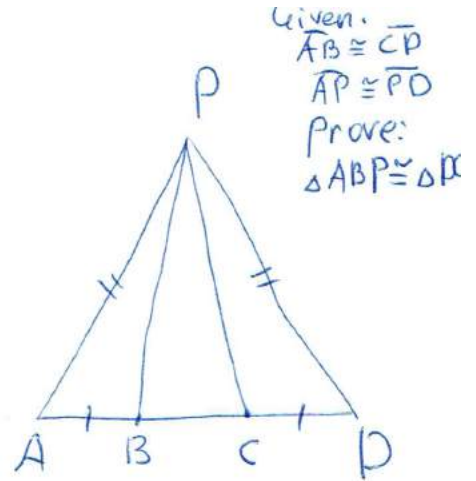
#3
P24

given
⑤ $\overline{AB} \cong \overline{CD}$

ITT
⑥ $\angle A \cong \angle D$

$\triangle ABP \cong \triangle DCP$

given
⑤ $\overline{AP} \cong \overline{PD}$



#5

given
 $\angle 1 \cong \angle 2$

ITT converse
 $\overline{JG} \cong \overline{JM}$

given
M is midpt. JK

def of midpt

$\overline{JM} \cong \overline{MK}$

Trans. prop
 $\overline{JG} \cong \overline{MK}$

